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APPOINTED UNDER THE CONVENTION BETWEEN THE UNITED STATES AND CANADA FOR THE PRESERVATION OF THE NORTHERN PACIFIC HALIBUT FISHERY

NUMBER 42

# MDRTALITY ESTIMATES FRDM TAGGING EXPERIMENTS DN PACIFIC HALIBUT 

## BY

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## FOREWORD

The Convention of 1953 between Canada and the United States for the preservation of the Halibut Fishery of the Northern Pacific Ocean and Bering Sea continued the conservation objectives of the three previous conventions, and requires that the stocks of halibut be developed to levels which will permit maximum sustained yield and that the stocks be maintained at those levels. These objectives require accurate knowledge of the effects of fishing upon the stocks.

This report presents estimates from tagging data of the fishing and total mortality rates experienced by halibut. Such estimates provide a basis for comparing and predicting the effects of fishing on different grounds and at different seasons and are necessary for the scientific management of the fishery.

# MORTALITY ESTIMATES FROM TAGGING <br> EXPERIMENTS ON PACIFIC HALIBUT <br> By 

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## INTRODUCTION

Management of a fishery requires knowledge of the effect of fishing upon the stocks of fish. The International Pacific Halibut Commission has used catch statistics, age composition data and tagging experiments to measure such effects. Conclusions supported by these three independent data sources warrant a degree of confidence that could not have been achieved from the analysis of tagging data alone.

The estimation of mortality rates of halibut from tagging data has been a continuing effort beginning with the work of Thompson and Herrington (1930). A number of methods of estimation have been attempted in the ensuing years. However, the one described herein appears to be the most satisfactory of those tested.

This report covers the estimation of the mortality rates from 60 tagging experiments conducted from 1925 to 1955 between Cape Scott, at the north end of Vancouver Island in British Columbia, and the Shumagin Islands in western Alaska, or between 60 -mile statistical areas 9 and 32 as shown in Figure 1. During this 30 -year period approximately 64,000 halibut were tagged and released in the region, over 14,700 of which were recovered by the end of 1963.

Total mortality and fishing mortality are estimated for each experiment. The relationship between the standard deviation of total mortality estimates and the number of fish tagged is examined and the optimum number of releases for a single tagging experiment is determined.

## TAGGING AND RECOVERY METHOD

The procedure for tagging and recovering tagged halibut was described in detail by Thompson and Herrington (1930) and is only briefly reviewed herein. To assure comparability the procedure has not been materially changed in the intervening years.

Halibut were caught by chartered fishing vessels using regular halibut setline gear except in the experiments conducted in 1947 when bottom trawl nets were used. The time and area of operations was specified by the Commission based upon the need for tagging data. The distribution of locations fished within the specified area tended to be more restricted when large catches were obtained and vice versa.

Usually 30 to 50 percent of the halibut were suitable for tagging based on a subjective appraisal of their viability. A monel metal strap tag was promptly attached on the dark or right side near the insertion of the operculum and the fish was forthwith returned to the sea. The date, location, length and apparent tagging injury were recorded with the tag number.

Tagged halibut were recovered for the most part by the setline halibut and blackcod fisheries, the bottomfish trawl fishery or the salmon troll fishery. Posters providing instructions for the reporting and return of tagged halibut were prominently displayed in all fish plants where halibut were landed. To encourage the reporting of recovered tags a reward of from fifty cents to two dollars was paid for the return of recovered tags, the amount of the reward depending upon the completeness of the recovery information. In addition, the finder was provided with information on the time and place of release of the recovered fish.

At the major halibut landing ports, Commission employees contacted halibut vessels at the completion of each trip to copy the fishing records and to redeem recaptured tagged halibut. Fish buyers and representatives of other governmental agencies cooperated by forwarding the recovered tags and information from ports where the Commission was not represented.


Figure 1. Pacific Coast of North America showing International Pacific Halibut Commission statistical areas

## METHOD OF ESTIMATION

The estimation of the mortality rates of halibut from tagging data is a two-stage process. The first stage involves the estimation of the mortality rates affecting the tagged individuals. The second stage involves the projection of these estimates to the total population from which the tagged individuals were taken. The distinction between the two stages is important because the assumptions employed in each are not the same.

Three basic methods are available for determining the mortality rates of marked fish. Ricker (1958) described a method in which the total mortality rate is estimated from the decline in recoveries with time. The total mortality rate is then partitioned into mortalities of two types, those attributable to fishing and those due to all other causes. The latter type of mortality is called the disappearance rate herein, a term which is synonymous with the 'other loss' of Beverton and Holt (1957). This separation of the two components of total mortality is based on the weighted average proportion of marked members recovered each year from the initial number of survivors of the previous year.

A second method in which the logarithm of the number of recoveries per unit of fishing effort is regressed against time was described by Gulland (1963). The use of linear regression analysis for estimating mortality rates from the decline in recoveries had been previously reported (Graham, 1938; Beverton and Holt, 1957; Chapman, 1961) but the method of Gulland is particularly well suited for halibut data. The slope of the regression line is the average total mortality rate and the intercept at the time of tagging is the logarithm of the expected number of initial recoveries per unit of fishing effort. The average catchability, which is defined as the average proportion of the stock that is caught by a standard unit of fishing effort, is estimated by dividing the value of the intercept by the number of marked individuals released. Fishing mortality is then obtained as the product of the catchability coefficient and the total fishing effort used.

A third method uses multiple regression analysis to compute the catchability coefficient and the disappearance rate separately (Chapman 1961). This method does not require that the number of marked individuals released be used in the calculation. However, pronounced changes in fishing effort between successive fishing periods and a constant catchability coefficient are required.

The multiple regression method is preferable from a theoretical standpoint but unrealistic estimates such as positive fishing and disappearance rates are frequently obtained with halibut data, even from large experiments. These anomalous results probably arise because of short term variations in the catchability coefficient. The same problems were encountered when the linear method of Beverton and Holt (1957) was used with halibut data and apparently for the same reasons.

The proportional and the linear regression methods of Ricker and Gulland respectively both yield satisfactory results with halibut data because short term variations in catchability tend to be compensatory over the long term. Of these two methods, the linear regression method was selected for use in this report because it provides variance estimates for the values of total mortality and catchability.

The linear regression model is derived from the basic equation

$$
\begin{equation*}
\frac{\mathbf{n}_{\mathbf{i}}}{\mathbf{f}_{\mathbf{i}}}=\frac{\mathrm{N}_{\mathrm{o}} \mathrm{q}}{\mathrm{Z}_{\mathrm{i}}}\left(\mathrm{e}^{-\mathrm{Z}_{\mathrm{i}}(\mathrm{i}-1)}\right)\left(1-\mathrm{e}^{-\mathrm{Z}_{\mathrm{i}}}\right) \tag{1}
\end{equation*}
$$

where n is the number of tags recovered, f is the number of units of effort fished, $\mathrm{N}_{\mathrm{o}}$ is the number of tags released, q is the catchability and Z is the total mortality. The subscripts refer to the $i^{\text {th }}$ interval which is one calendar year throughout this report. The definition of catchability used herein is more general than that used by some other authors in that unequal vulnerability of different stock components is recognized.

The approximation,

$$
\begin{equation*}
\left(1-e^{-Z_{i}}\right)=Z_{i}\left(e-\frac{Z_{i}}{2}\right) \tag{2}
\end{equation*}
$$

is reasonable when $\mathrm{Z}_{\mathrm{i}}$ is small (Chapman, 1961). Even with $\mathrm{Z}_{\mathrm{i}}$ as large as 1.0 , the righthand side of equation (2) is within four percent of the left-hand side. Substituting the above approximation into equation (1) yields the equation

$$
\begin{equation*}
\frac{n_{i}}{f_{i}}=N_{o q e}-\mathrm{Z}_{\mathrm{i}}(\mathrm{i}-0.5) \tag{3}
\end{equation*}
$$

Converting to logarithms and substituting $Z$ for $Z_{i}$ yields

$$
\begin{equation*}
\operatorname{Ln} \frac{n_{i}}{f_{i}}=\operatorname{Ln}\left(\mathrm{N}_{0} \mathrm{q}\right)-\mathrm{Z}(\mathrm{i}-0.5)+\varepsilon \tag{4}
\end{equation*}
$$

where Z is the arithmetic average of all $\mathrm{Z}_{\mathrm{i}}$ and $\varepsilon$ is the error term which is assumed to be normally distributed and to have an expected value of zero.

The substitution of $Z$ for $Z_{i}$ is necessary to satisfy the requirements for linear regression. Since $f_{i}$ is known to vary and $q$ and the disappearance rate are assumed to be constant then $Z_{i}$ will vary with $f_{i}$. Most of the effect of annual variation in $f_{i}$ is eliminated when the number of recoveries in each year is divided by the corresponding $f_{i}$. Residual effects of varying $f_{i}$ will appear in the error term provided no trend in $f_{i}$ exists. If $f_{i}$ increases or decreases during the course of the experiment, small errors in q and Z may result.

The probable magnitude of the errors of this type was examined by calculating estimates of q and Z from trial data involving varying levels of effort. The greatest error in q of 16 percent was obtained when effort in recovery years two through five was double that in recovery year one. In the same trial the error in Z was only five percent. Changes in effort observed in the experiments described herein were smaller than that used in the above trial. Therefore, errors in estimates of $q$ and $Z$ due to changing effort are expected to be small in most cases and to be less than 16 and 5 percent respectively for any experiment.

Equation (4) contains two constant unknowns, $\operatorname{Ln}\left(N_{o} q\right)$ and $Z$ which are estimated from the intercept and slope respectively from linear regression analysis. The value of $q$ is obtained algebraically from $\operatorname{Ln}\left(\mathrm{N}_{0} \mathrm{q}\right)$ since $\mathrm{N}_{0}$ is known from the number of tagged fish originally released. Of course, $q$ would be underestimated if some of the tagged fish die or lose their tags shortly after tagging but the estimate of $Z$ would be unaffected. Live-box experiments were conducted in 1958 to test for tagging mortality. Mortalities during the first two weeks after tagging were estimated to be five percent or less and most deaths due to tagging appeared to have occurred by that time (Peltonen, Ms.).

Non-reporting of tags which causes the loss of a proportion of each group of recaptures will also result in the underestimation of q. Non-reporting loss of tags can occur for a variety of reasons and does not necessarily imply indifference on the part of persons who recapture tagged halibut. Myhre (1966) used double-tag experiments
to measure non-reporting loss as well as shedding loss. Non-reporting losses were estimated to be 0.04 of recaptured tags but losses that operated on both tags jointly could not be measured by this technique. Thus losses due to non-reporting of tags could be greater than 0.04 .

The value of Z in equation (4) is the average total mortality rate for the experiment and includes all factors which cause tagged fish to decrease in numbers with time. Two important components of total mortality are fishing and natural mortality. Also included will be any shedding of tags which occurs continuously during the course of the experiment.

The estimation of total mortality requires constant catchability of the tagged fish. If this condition is not satisfied, total mortality will be overestimated or underestimated depending upon whether the tagged fish become more or less catchable with time.

The estimates of fishing and total mortality are affected by the manner of dealing with migrant tagged fish. If migration did not alter the chances of recovering tagged fish, such migrants could be included as usable recoveries as if they had remained in the tagging area and the decline in numbers would be a valid indicator of total mortality. In practice, fishing mortality varies from area to area so this solution would be approximate at best. A second alternative would be to exclude migrant recoveries in which case migration out of the area could become an important part of the disappearance rate and the fishing mortality estimates obtained would reflect the utilization of non-migrant tagged fish only.

A third alternative, and the one used in this report, is to calculate the $n_{i} / f_{i}$ for each statistical area. These values are then summed over all statistical areas to obtain the desired statistic for the dependent variable in equation (4). The estimates of fishing and total mortality thus obtained closely approximate the rates to which the tagged fish would have been exposed if emigration did not occur.

Since the amount of fishing area differs between recovery areas, gear density is used as the index of fishing intensity. Gear density is proportional to the effective overall fishing intensity of Beverton and Holt (1957) and is defined as the weighted mean number of standard units fished per square nautical mile per year.

The gear density for the $j^{\text {th }}$ area in the $i^{\text {th }}$ year is given by the equation $g_{i j}=\frac{f_{i j}}{A_{j}}$ where $A_{j}$ is the bottom area in the $j^{\text {th }}$ statistical area. The mean gear density for an experiment in the $i^{\text {th }}$ year depends upon the number of recoveries taken from each of the k areas in that year as shown by the equation

$$
\begin{equation*}
\overline{\mathrm{g}}_{\mathrm{i}}=\frac{\sum_{\mathrm{j}=1}^{\mathrm{k}} \mathrm{n}_{\mathrm{ij}}}{\sum_{\mathrm{j}=1}^{\mathrm{k}}\left(\frac{\mathrm{n}_{\mathrm{i}}}{\mathrm{~g}_{\mathrm{i}}}\right)_{\mathrm{j}}} \tag{5}
\end{equation*}
$$

Bottom area is defined as the amount of bottom in square nautical miles over which halibut and halibut gear are distributed. Preferably allowance should also be made for non-uniform distribution of fishing gear but detailed data on distribution of effort were not available for all years and areas employed in this report. Myhre (1963) measured the bottom area for statistical areas 9 to 32 using a planimeter and charts published by the United States Coast and Geodetic Survey or by the United States Hydrographic Office. These calculations which have been repeated and extended to statistical area 36 are given in the following table.

| Statistical Area | Bottom Area* in Square Miles | Statistical Area | Bottom Area* in Square Miles |
| :---: | :---: | :---: | :---: |
| 9 | 2960 | 23 | 2990 |
| 10 | 3980 | 24 | 3350 |
| 11 | 3200 | 25 | 4900 |
| 12 | 2360 | 26 | 7940 |
| 13 | 370 | 27 | 5200 |
| 14 | 2950 | 28 | 4410 |
| 15 | 2120 | 29 | 6030 |
| 16 | 1390 | 30 | 5710 |
| 17 | 2320 | 31 | 4770 |
| 18 | 2580 | 35 | 350 |
| 19 | 2560 | 34 | 2630 |
| 20 | 1550 | 35 | 2400 |
| 21 | 1370 | 36 | 1730 |
| 22 |  |  |  |

*The bottom areas differ from those given in Myhre (1963) but should be considered as more precise.
Incorporating both the utilization of migrants and the gear density concept in equation (4) yields the relationship

$$
\begin{equation*}
\operatorname{Ln} \sum_{j=1}^{\mathrm{k}}\left(\frac{\mathrm{n}_{\mathrm{i}}}{\overline{\mathrm{~g}_{\mathrm{i}}}}\right)_{\mathrm{j}}=\operatorname{Ln}\left(\mathrm{N}_{o} \mathrm{q}\right)-\mathrm{Z}(\mathrm{i}-0.5)+\varepsilon \tag{6}
\end{equation*}
$$

which is the one used for the estimation of Z and q . Since the total number of annual recoveries, $\sum_{j=1}^{k} n_{i j}$ is expected to decrease with increase in $i$, the dependent variable (left-hand side of equation 6) was weighted by $n_{i}$. Further justification for this weighting procedure is given in a later section of this report.

## DATA USED

Most of the fish tagged from 1925 to 1955 could be grouped into experiments according to time and place of tagging. Some experiments were unsatisfactory for the estimation of mortality rates because they produced too few recoveries or because recoveries were not obtained over at least three full recovery years. A total of 60 experiments that could be used for the estimation of mortality rates are listed in Table 1 which shows the year and the statistical area or areas of tagging.

The month of tagging varies considerably from experiment to experiment and some experiments include tagged fish that were released over a period of two or three months. Since the method to be used for estimating catchability requires definition of the specific time of tagging, a weighted mean time of tagging $\left(\mathrm{M}_{\mathrm{t}}\right)$ was determined for each experiment using the equation

$$
\begin{equation*}
M_{t}=\frac{\sum_{i=1}^{k} T_{i} d_{i}}{365 \mathrm{~T} .} \tag{7}
\end{equation*}
$$

where $\mathrm{d}_{\mathrm{i}}$ is the $\mathrm{i}^{\text {th }}$ day of the year, $\mathrm{T}_{\mathrm{i}}$ is the number of fish tagged on that day and T . is the total number of fish tagged in the experiment.

January 1 of the year of tagging is defined as zero time and the year of tagging is defined as the zero year. The midpoint of fishing and, hence, of recovery was usually at about mid-May or at about 0.45 of the way through the year. Although the length of the fishing season was considerably reduced from the early to the more recent years, the midpoint of fishing changed little because the opening date was set later in the
year as the length of the season declined. The midpoint of recovery in the first and subsequent recovery years of each experiment is therefore defined as $1.45,2.45$ and so on. Variations from these midpoints are considered small enough to satisfy the requirements of the fixed regression model.

Most of the experiments included some tagged fish that were too small to be fully available to halibut gear at the time of tagging. Both the modal size of the fish tagged and the percentage recovery during the first full recovery year by size at tagging were used to determine the size of full recruitment for fish released in each experiment.

Differences in modal size between experiments that were similar with respect to area and year were smoothed visually to overcome statistical variations. When the division occurred within a size-class, the entire class was considered to be fully recruited in anticipation of some additional growth during the remainder of the zero year. The number of fish tagged in each experiment by length class and the separation of pre-recruits and full recruits (vertical line) is given in Table 2.

Area 2 fish are seen to be fully recruited at a smaller size than Area 3 fish and fish tagged in the 1920's in both areas were found to be fully recruited at a smaller size than those tagged in more recent years. Recruitment is usually thought to be a

Table 1. Year, month and statistical area of tagging for 60 experiments conducted from 1925 to 1955.

| Experiment Number | Year | Month | Statistical Areas | Experiment Number | Year | Month | Statistical Areas |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1925 | JuneAugust | 12,13 | 30 | 1951 | July | 27-29 |
|  |  |  |  | 31 | 1951 | August | 20, 21 |
| 2 | 1925 | July | 11 | 32 | 1951 | AugustSeptember | 13 |
| 3 | 1925 | June | 13 |  |  |  |  |
| 4 | 1925 | August | 15 | 33 | 1951 | September | 11 |
| 5 | 1926 | June | 10 | 34 | 1951 | SeptemberOctober | 10 |
| 6 | 1926 | July | 13 |  |  |  |  |
| 7 | 1926 | JulyAugust | 15 | 35 | 1952 | MarchApril | 9 |
| 8 | 1926 | NovemberDecember | 20 | 36 | 1952 | April | 1325,26 |
|  |  |  |  | 37 | 1952 | May |  |
| 9 | 1927 | November | 25 | 38 | 1952 | May | 27 |
| 10 | 1927 | December | 22 | 39 | 1952 | June- | 11 |
| 11 | 1929 | AprilMay | 32 |  |  | July June- |  |
| 12 | 1933 | FebruaryMarch | 11 | 40 | 1952 | JuneJuly | 13 |
|  |  |  |  | 41 | 1953 | April | 13 |
| 13 | 1933 | JanuaryFebruary | 20, 22 | $\begin{aligned} & 42 \\ & 43 \end{aligned}$ | $\begin{aligned} & 1953 \\ & 1953 \end{aligned}$ | May April- | 1312 |
|  |  |  |  |  |  |  |  |
| 14 | 1933 | December | 24, 25 |  |  | May |  |
| 15 | 1933 | December | 21, 22 | 44 | 1953 | MayJuly | 11 |
| 16 | 1935 | May- | 10 |  |  |  |  |
|  |  | June |  | 45 | 1953 | June | 10 |
| 17 | 1935 | May | 9 | 46 | 1953 | July | 9 |
| 18 | 1936 | May | 10 | 47 | 1953 | June | 15 |
| 19 | $\begin{aligned} & 1939- \\ & 1940 \end{aligned}$ | DecemberJanuary | 11 | 48 | 1953 | July | 13 |
|  |  |  |  | 49 | 1954 | May | 25 |
| 20 | 1940 | NovemberDecember | 16,17 | 50 | 1954 | MayJune | 28 |
| 21 | 1947 | May- | 10 | 51 | 1954 | June | 20, 21 |
|  |  | June |  | 52 | 1954 | JuneJuly | 25, 26 |
| 22 | 1947 | June | 13 |  |  |  |  |
| 23 | 1947 | June | 13 | 53 | 1954 | August | 20, 21 |
| 24 | 1947 | June | 9 | 54 | 1955 | July | 10 |
| 25 | 1949 | July- | 26,27 | 55 | 1955 | August | 13 |
|  |  | August |  | 56 | 1955 | August | 15 |
| 26 | 1949 | JulySeptember | 13 | 57 | 1955 | AugustSeptember | 13 |
| 27 | 1950 | August- | 28, 29 | 58 | 1955 | September | 11,12 |
|  |  | September |  | 59 | 1955 | September- |  |
| 28 | 1950 | September |  |  |  | October |  |
| 29 | 1951 | FebruaryApril | 17,18 | 60 | 1955 | NovemberDecember | 20-22 |

Table 2. Length frequency of all fish tagged and size of full recruitment (vertical line) of fish in each experiment.

| Length in Centimeters |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Experiment Number | $<50$ | $\begin{aligned} & 50- \\ & 54 \end{aligned}$ | $\begin{aligned} & 55- \\ & 59 \end{aligned}$ | $\begin{aligned} & 60- \\ & 64 \end{aligned}$ | $\begin{aligned} & 65- \\ & 69 \end{aligned}$ | $\begin{aligned} & 70- \\ & 74 \end{aligned}$ | $\begin{aligned} & 75- \\ & 79 \end{aligned}$ | $\begin{aligned} & 80- \\ & 84 \end{aligned}$ | $\begin{aligned} & 85- \\ & 89 \end{aligned}$ | $\begin{aligned} & 90- \\ & 94 \end{aligned}$ | $\begin{aligned} & 95- \\ & 99 \end{aligned}$ | $\begin{aligned} & 100- \\ & 104 \end{aligned}$ | $\begin{aligned} & 105- \\ & 109 \end{aligned}$ | $\begin{aligned} & 110- \\ & 114 \end{aligned}$ | $\begin{aligned} & 115- \\ & 119 \end{aligned}$ | $\begin{aligned} & 120- \\ & 124 \end{aligned}$ | $\begin{aligned} & 125- \\ & 129 \end{aligned}$ | $\geq 130$ |
| 1 | 9 | 18 | 74 | 107 | 68 | 44 | 26 | 11 | 6 | 3 | 5 | 4 | 3 | 3 | 0 | 0 | 1 | 4 |
| 2 | 15 | 21 | 46 | 46 | 64 | 37 | 28 | 19 | 9 | 7 | 0 | 5 | 2 | 1 | 0 | 1 | 0 | 2 |
| 3 | 9 | 27 | 59 | 107 | 147 | 99 | 76 | 21 | 20 | 13 | 14 | 4 | 4 | 4 | 1 | 1 | 0 | 2 |
| 4 | 2 | 1 | 6 | 23 | 36 | 20 | 8 | 6 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 5 | 7 | 77 | 232 | 384 | 372 | 245 | 81 | 45 | 28 | 25 | 10 | 5 | 2 | 1 | 0 | 1 | 0 | 1 |
| 6 | 8 | 28 | 37 | 91 | 70 | 17 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 7 | 36 | 89 | 259 | 370 | 296 | 120 | 48 | 13 | 9 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 8* | 0 | 0 | 4 | 28 | 151 | 271 | 264 | 216 | 237 | 240 | 172 | 91 | 39 | 24 | 9 | 1 | 0 | 0 |
| 9* | 3 | 4 | 37 | 111 | 170 | 190 | 143 | 137 | 121 | 102 | 69 | 38 | 21 | 12 | 7 | 0 | 0 | 0 |
| 10* | 0 | 2 | 2 | 35 | 96 | 173 | 161 | 168 | 166 | 161 | 143 | 105 | 72 | 32 | 13 | 7 | 1 | 1 |
| 11 * | 2 | 13 | 39 | 100 | 177 | 139 | 135 | 79 | 59 | 50 | 26 | 28 | 22 | 10 | 7 | 4 | 2 | 7 |
| 12 | 0 | 0 | 3 | 20 | 53 | 86 | 71 | 59 | 36 | 31 | 19 | 13 | 11 | 5 | 5 | 4 | 1 | 13 |
| 13* | 0 | 1 | 3 | 10 | 21 | 47 | 42 | 40 | 25 | 32 | 22 | 18 | 15 | 21 | 10 | 11 | 10 | 12 |
| 14* | 0 | 1 | 8 | 16 | 30 | 26 | 22 | 22 | 13 | 10 | 9 | 14 | 10 | 9 | 9 | 10 | 10 | 24 |
| 15* | 0 | 0 | 0 | 3 | 16 | 29 | 31 | 27 | 20 | 21 | 26 | 11 | 8 | 6 | 10 | 7 | 3 | 21 |
| 16 | 0 | 0 | 5 | 16 | 38 | 73 | 82 | 70 | 31 | 30 | 14 | 14 | 8 | 7 | 3 | 1 | 0 | 0 |
| 17 | 0 | 0 | 2 | 7 | 25 | 47 | 37 | 36 | 9 | 12 | 6 | 5 | 3 | 2 | 3 | 4 | 2 | 2 |
| 18 | 0 | 2 | 29 | 40 | 66 | 84 | 74 | 56 | 25 | 20 | 16 | 6 | 8 | 7 | 1 | 0 | 5 | 3 |
| 19 | 0 | 0 | 3 | 8 | 32 | 56 | 88 | 62 | 76 | 83 | 70 | 58 | 51 | 65 | 43 | 45 | 22 | 94 |
| 20 | 0 | 3 | 11 | 11 | 29 | 34 | 33 | 23 | 17 | 16 | 6 | 11 | 15 | 14 | 14 | 29 | 19 | 88 |
| 21 | 7 | 100 | 230 | 334 | 477 | 472 | 300 | 182 | 100 | 53 | 28 | 7 | 13 | 8 | 5 | 2 | 4 | 9 |
| 22 | 7 | 14 | 25 | 66 | 54 | 51 | 26 | 14 | 8 | 9 | 0 | 1 | 1 | 0 | 0 | 3 | 0 | 2 |
| 23 | 16 | 34 | 48 | 88 | 154 | 154 | 79 | 30 | 11 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 2 |
| 24 | 0 | 0 | 0 | 12 | 79 | 109 | 57 | 28 | 7 | 5 | 3 | 4 | 1 | 2 | 0 | 0 | 0 | 1 |
| 25* | 10 | 13 | 31 | 66 | 91 | 148 | 142 | 143 | 93 | 54 | 39 | 37 | 19 | 35 | 37 | 46 | 41 | 203 |
| 26 | 0 | 0 | 4 | 38 | 105 | 228 | 219 | 199 | 99 | 60 | 38 | 29 | 21 | 35 | 9 | 12 | 9 | 39 |
| 27* | 3 | 7 | 40 | 65 | 70 | 82 | 84 | 93 | 74 | 104 | 93 | 84 | 95 | 59 | 59 | 59 | 33 | 57 |
| 28 | 0 | 0 | 1 | 4 | 10 | 27 | 51 | 51 | 40 | 36 | 31 | 17 | 14 | 4 | 1 | 2 | 1 | 3 |
| 29 | 3 | 12 | 43 | 84 | 115 | 141 | 119 | 163 | 115 | 96 | 70 | 104 | 92 | 71 | 69 | 68 | 65 | 258 |
| 30* | 8 | 17 | 20 | 51 | 68 | 91 | 96 | 116 | 92 | 65 | 61 | 72 | 70 | 70 | 54 | 63 | 57 | 107 |

* Area 3 experiment.

Table 2.- (continued)

| Length in Centimeters |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Experiment Number | $<50$ | $\begin{aligned} & 50- \\ & 54 \end{aligned}$ | $\begin{aligned} & 55- \\ & 59 \end{aligned}$ | $\begin{aligned} & 60- \\ & 64 \end{aligned}$ | $\begin{aligned} & 65- \\ & 69 \end{aligned}$ | $\begin{aligned} & 70- \\ & 74 \end{aligned}$ | $\begin{aligned} & 75- \\ & 79 \end{aligned}$ | $\begin{aligned} & 80- \\ & 84 \end{aligned}$ | $\begin{aligned} & 85- \\ & 89 \end{aligned}$ | $\begin{aligned} & 90- \\ & 94 \end{aligned}$ | $\begin{aligned} & 95- \\ & 99 \end{aligned}$ | $\begin{aligned} & 100- \\ & 104 \end{aligned}$ | $\begin{aligned} & 105- \\ & 109 \end{aligned}$ | $\begin{aligned} & 110- \\ & 114 \end{aligned}$ | $\begin{aligned} & 115- \\ & 119 \end{aligned}$ | $\begin{aligned} & 120- \\ & 124 \end{aligned}$ | $\begin{aligned} & 125- \\ & 129 \end{aligned}$ | $\geq 130$ |
| 31* | 0 | 1 | 6 | 16 | 38 | 82 | 121 | 170 | 210 | 184 | 171 | 147 | 117 | 89 | 71 | 40 | 23 | 16 |
| 32 | 1 | 1 | 9 | 50 | 139 | 268 | 301 | 306 | 216 | 173 | 88 | 79 | 45 | 41 | 30 | 23 | 13 | 37 |
| 33 | 0 | 0 | 0 | 5 | 14 | 23 | 14 | 16 | 30 | 13 | 17 | 5 | 11 | 10 | 7 | 7 | 10 | 22 |
| 34 | 0 | 0 | 3 | 38 | 167 | 317 | 467 | 512 | 416 | 271 | 185 | 115 | 74 | 47 | 45 | 13 | 17 | 22 |
| 35 | 0 | 0 | 4 | 14 | 45 | 111 | 118 | 99 | 80 | 67 | 48 | 40 | 31 | 32 | 32 | 16 | 13 | 22 |
| 36 | 0 | 0 | 0 | 11 | 38 | 74 | 119 | 93 | 51 | 30 | 18 | 10 | 7 | 8 | 2 | 2 | 7 | 8 |
| 37* | 0 | 5 | 22 | 33 | 65 | 64 | 66 | 56 | 56 | 68 | 63 | 75 | 59 | 42 | 47 | 36 | 46 | 94 |
| 38* | 6 | 9 | 27 | 40 | 58 | 57 | 34 | 22 | 20 | 25 | 19 | 12 | 26 | 24 | 27 | 16 | 20 | 51 |
| 39 | 0 | 0 | 0 | 3 | 8 | 16 | 24 | 39 | 34 | 42 | 39 | 54 | 52 | 50 | 50 | 56 | 45 | 146 |
| 40 | 0 | 2 | 1 | 2 | 13 | 27 | 44 | 68 | 55 | 49 | 50 | 44 | 37 | 44 | 28 | 21 | 21 | 200 |
| 41 | 0 | 10 | 13 | 14 | 18 | 34 | 56 | 75 | 57 | 51 | 50 | 50 | 38 | 43 | 36 | 31 | 26 | 48 |
| 42 | 0 | 2 | 0 | 6 | 23 | 94 | 130 | 142 | 117 | 66 | 44 | 30 | 17 | 8 | 6 | 1 | 4 | 2 |
| 43 | 0 | 1 | 8 | 23 | 41 | 120 | 181 | 188 | 130 | 105 | 61 | 34 | 18 | 11 | 9 | 6 | 2 | 6 |
| 44 | 10 | 10 | 38 | 68 | 80 | 159 | 225 | 254 | 224 | 224 | 244 | 194 | 173 | 135 | 96 | 71 | 50 | 87 |
| 45 | 0 | 0 | 0 | 3 | 10 | 26 | 36 | 43 | 36 | 23 | 9 | 2 | 1 | 1 | 1 | 0 | 0 | 0 |
| 46 | 0 | 0 | 0 | 1 | 4 | 10 | 33 | 29 | 19 | 18 | 8 | 9 | 4 | 3 | 0 | 1 | 0 | 0 |
| 47 | 3 | 25 | 49 | 78 | 123 | 115 | 114 | 83 | 62 | 38 | 34 | 26 | 34 | 22 | 25 | 34 | 26 | 75 |
| 48 | 0 | 0 | 1 | 1 | 5 | 12 | 12 | 17 | 29 | 22 | 18 | 17 | 8 | 10 | 3 | 3 | 5 | 10 |
| 49* | 0 | 0 | 0 | 1 | 20 | 28 | 26 | 25 | 32 | 39 | 36 | 65 | 48 | 66 | 69 | 86 | 56 | 138 |
| 50* | 0 | 0 | 0 | 0 | 17 | 22 | 31 | 25 | 33 | 18 | 16 | 32 | 35 | 37 | 43 | 45 | 36 | 95 |
| 51* | 0 | 0 | 0 | 0 | 36 | 54 | 68 | 59 | 49 | 57 | 67 | 76 | 63 | 52 | 47 | 35 | 27 | 51 |
| 52* | 0 | 0 | 0 | 0 | 38 | 37 | 36 | 33 | 31 | 21 | 15 | 24 | 22 | 35 | 34 | 34 | 28 | 121 |
| 53* | 0 | 0 | 0 | 0 | 24 | 43 | 44 | 55 | 51 | 66 | 75 | 109 | 85 | 94 | 88 | 55 | 51 | 119 |
| $54$ | 0 | 0 | 0 | 0 | 95 | 233 |  | 310 | 278 | 201 | 117 | 98 | 89 | 79 | 48 | 41 | 39 | 80 |
| 55 | 0 | 0 | 0 | 0 | 32 | 48 | 82 | 113 | 120 | 113 | 141 | 110 | 100 | 85 | 81 | 68 | 67 | 177 |
| 56 | 0 | 0 | 0 | 0 | 125 | 188 | 219 | 167 | 132 | 91 | 88 | 56 | 40 | 46 | 41 | 38 | 25 | 144 |
| 57 | 0 | 0 | 0 | 0 | 153 | 324 | 476 | 547 | 347 | 204 | 77 | 61 | 45 | 44 | 42 | 33 | 30 | 152 |
| 58 | 0 | 0 | 0 | 0 | 18 | 59 | 60 | 51 | 33 | 23 | 20 | 26 | 12 | 22 | 17 | 15 | 15 | 21 |
| 59 | 0 | 0 | 0 | 0 | 69 | 174 | 167 | 125 | 78 | 48 | 37 | 29 | 29 | 22 | 22 | 19 | 22 | 60 |
| $60^{*}$ | 0 | 0 | 0 | 3 | 27 | 57 | 48 | 57 | 49 | 53 | 49 | 67 | 68 | 81 | 84 | 104 | 84 | 411 |

* Area 3 experiment.
characteristic of the gear rather than the fish but the above differences could not be attributed to gear diversities.

To determine the amount of bias that might result from the inclusion of incompletely recruited individuals in the data used to estimate $q$ and $Z$, four experiments were analyzed with and without pre-recruits. The following table summarizes the result of this comparison:

|  | Without Pre-recruits |  | With Pre-recruits |  |
| :---: | :---: | :---: | :---: | :---: |
| Experiment | q | Z | q |  |
| 30 | 0.012 | 0.48 | 0.011 | 0.50 |
| 31 | 0.019 | 0.39 | 0.018 | 0.40 |
| 44 | 0.045 | 0.61 | 0.044 | 0.61 |
| 54 | 0.030 | 0.57 | 0.030 | 0.58 |

The changes in $q$ and $Z$ resulting from inclusion of all pre-recruits are small and may even result from changes in sample size. Thus it is concluded that for halibut the determination of the point of full recruitment is not a critical matter in the estimation of $q$ and $Z$.

The mean time of tagging, the minimum size of full recruitment and the number of fully recruited fish tagged are given for each experiment in Table 3.

Zero-year recoveries must be omitted from mortality calculations because the availability of tagged halibut in that year is frequently atypical of subsequent years. Occasionally this condition carries over to the first full recovery year. At least two

Table 3. Mean time of tagging, size at full recruitment and number of fully recruited fish tagged in each experiment.

| Experiment number | Mean tagging time | Size at full recruitment (cm) | Number of fully recruited fish tagged | Experiment number | Mean tagging time | Size at full recruitment (cm) | Number of fully recruited fish tagged |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | . 55 | 60 | 285 | 31* | . 60 | 80 | 1238 |
| 2 | . 53 | 60 | 221 | 32 | . 69 | 75 | 1352 |
| 3 | . 46 | 60 | 513 | 33 | . 67 | 75 | 162 |
| 4 | . 61 | 60 | 94 | 34 | . 75 | 75 | 2184 |
| 5 | . 46 | 60 | 1200 | 35 | . 26 | 75 | 598 |
| 6 | . 54 | 60 | 180 | 36 | . 32 | 75 | 355 |
| 7 | . 58 | 60 | 856 | 37* | . 38 | 80 | 642 |
| 8* | . 92 | 65 | 1715 | 38* | . 40 | 80 | 262 |
| 9* | . 87 | 65 | 1010 | 39 | . 48 | 75 | 631 |
| 10* | . 94 | 65 | 1299 | 40 | . 51 | 75 | 661 |
| 11* | . 34 | 65 | 745 | 41 | . 30 | 75 | 561 |
| 12 | . 18 | 65 | 407 | 42 | . 36 | 75 | 567 |
| 13* | . 04 | 70 | 305 | 43 | . 37 | 75 | 751 |
| 14* | . 95 | 70 | 188 | 44 | . 48 | 75 | 1977 |
| 15* | . 96 | 70 | 220 | 45 | . 44 | 75 | 152 |
| 16 | . 42 | 70 | 333 | 46 | . 54 | 75 | 124 |
| 17 | . 41 | 70 | 168 | 47 | . 48 | 75 | 568 |
| 18 | . 38 | 70 | 305 | 48 | . 50 | 75 | 154 |
| 19 | . 01 | 70 | 813 | 49* | . 37 | 80 | 660 |
| 20 | .91 | 70 | 319 | 50* | . 40 | 80 | 415 |
| 21 | . 41 | 70 | 1183 | 51* | . 46 | 80 | 583 |
| 22 | . 45 | 70 | 115 | 52* | . 51 | 80 | 398 |
| 23 | . 45 | 70 | 279 | 53* | . 64 | 80 | 848 |
| 24 | . 47 | 70 | 217 | 54 | . 56 | 75 | 1634 |
| 25* | . 60 | 70 | 1037 | 55 | . 60 | 75 | 1257 |
| 26 | . 67 | 70 | 997 | 56 | . 63 | 75 | 1087 |
| $27 *$ | . 67 | 70 | 976 | 57 | . 67 | 75 | 2058 |
| 28 | . 72 | 70 | 278 | 58 | . 71 | 75 | 315 |
| 29 | . 20 | 75 | 1290 | 59 | . 74 | 75 | 658 |
| 30* | . 56 | 75 | 923 | 60* | . 89 | 80 | 1107 |

* Area 3 experiment.
reasons for this difference are known at present. First, some or all of the zero-year fishing effort may have been expended before the tagged fish were released. Second, tagged halibut appear to be relatively unavailable to the fishery for up to 3 months after tagging. This phenomenon is illustrated by experiments 17 and 18 which were conducted on the Goose Islands grounds in May of 1935 and 1936 respectively. The increasing availability of these tagged fish, as shown by the number of recoveries taken per thousand skates of gear fished, is shown in the following table.

|  | Experiment 17 |  |  |  |  |  | Experiment 18 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

Elimination of zero-year recoveries poses no particular problem in the estimation of catchability by the linear regression method. However, if the expected number of recoveries based on the survival slope were not taken by fishing in the zero-year, as was usually the case, the number of tagged fish surviving to the start of the first recovery year would be greater than expected and a positive bias in the catchability estimate would result. An iterative process is used to calculate the effective number of fish tagged in the experiment which is the number that would have had to have been released to obtain the number of recoveries per unit effort in years one and following if zero-year recoveries had been a uniform part of that series. Three steps in the iterative process were usually sufficient to obtain successive estimates within one fish of each other.

Recoveries by trawl net gear are excluded because fishing for halibut by trawl net is prohibited by the Commission's regulations. Hence, in this analysis the tagged and untagged populations are presumed to suffer no trawl net fishing mortality. Trawl fishermen are encouraged to turn in tagged fish but since these are excluded from the analysis, recovery of tagged fish by trawlers will appear as a component of the disappearance rate and not as fishing mortality.

The distribution of recoveries by statistical area and year of recovery is given in Table 4. Recoveries from statistical areas below area 9 are shown in the table but excluded from the totals and from the analyses. In each experiment recoveries such as those in the zero year which were not used in calculating the regression line are separated from all others by a horizontal line but are included in the totals. Also for each experiment bold type is used to indicate recoveries in the statistical area or areas of tagging.

The calculated number of standard skates* of setline gear fished in statistcial areas 9 to 36 for the years 1926-1963 is given in Table 5. These data were calculated by dividing the total catch by the average catch per skate for each area in each year. The average catch per skate was obtained from fishing records made available to the Commission by operators of the individual fishing vessels.

[^0]Table 4. Distribution of recoveries by statistical area and year of recovery.


Table 4.-(continued).


Table 4.-(continued).


Table 4.-(continued).

| Experiment Number | Recovery Year | $<9$ | 9 | 10 | 0 | 11 | 12 | 13 |  | 14 | 15 | 16 | 17 | 18 | 19 | 20 | STAT 21 | STI | AL | $\begin{gathered} \overline{\mathrm{REA}} \\ 24 \end{gathered}$ | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | Total 9-36 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 16 | 0 |  |  | 23 | 30 |  |  |  |  |  |  |  |  |  | 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 33 |
|  | $\begin{aligned} & 1 \\ & 1 \\ & 2 \\ & 3 \\ & 4 \\ & 4 \\ & 6 \\ & 7 \\ & 8 \\ & 9 \end{aligned}$ | $\begin{aligned} & 2 \\ & 1 \\ & 1 \end{aligned}$ |  | $\begin{array}{ll} 9 & \mathbf{3} \\ 2 & 26 \\ 2 & 22 \\ 1 & 18 \end{array}$ |  | $\frac{1}{2}$ <br> 1 <br> 1 | 1 <br> 1 | 1 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 45 <br> 30 <br> 26 <br> 20 <br> 10 <br> 9 <br> 5 <br> 1 <br> 1 |
|  |  | 4 |  | 15 | 52 | 5 | 3 | 2 |  |  |  |  |  |  | 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 180 |
| 17 | 0 | 1 |  | 4 | 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 5 |
|  | $\begin{aligned} & \hline 1 \\ & 2 \\ & 3 \\ & 4 \\ & 5 \\ & 6 \end{aligned}$ | 1 | $\begin{aligned} & 21 \\ & 11 \end{aligned}$ |  | $\begin{aligned} & 3 \\ & 2 \\ & 1 \\ & 2 \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  | 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $\begin{array}{r}24 \\ 14 \\ 14 \\ 4 \\ 4 \\ 4 \\ \hline\end{array}$ |
|  |  | 2 | 5 | 4 | 9 | 2 |  |  |  |  |  |  |  |  |  |  | 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 66 |
| 18 | 0 |  |  | 215 | 15 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 17 |
| Total | $\begin{aligned} & 1 \\ & \frac{1}{2} \\ & 3 \\ & 4 \\ & 5 \\ & 6 \\ & 7 \\ & 7 \end{aligned}$ | 1 |  | $\begin{array}{ll}9 & 3 \\ 8 & 1 \\ 4 & 1\end{array}$ | $\begin{array}{r} 34 \\ 13 \\ 13 \\ 7 \\ 3 \\ 1 \\ 1 \end{array}$ | 2 <br> 1 | 1 1 | 1 1 |  |  |  | $\frac{1}{1}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $\begin{array}{r}16 \\ 22 \\ 19 \\ 10 \\ 3 \\ 1 \\ 1 \\ 1 \\ \hline\end{array}$ |
|  |  | 1 | 2 | 4 | 87 | 3 | 2 | 2 |  |  |  | 2 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 120 |
| 19 | 0 | 6 |  | 41 | 16 | 23 | 5 | 2 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 60 |
| Total | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \\ & 4 \\ & 5 \\ & 6 \\ & 7 \end{aligned}$ | 1 1 2 1 |  |  | $\begin{array}{r} 19 \\ 11 \\ 4 \\ 1 \\ 1 \\ 1 \\ \hline \end{array}$ | $\begin{array}{r} 17 \\ 8 \\ 3 \\ 2 \\ 2 \end{array}$ | $\begin{aligned} & \hline 5 \\ & 4 \\ & 4 \\ & 1 \end{aligned}$ |  |  | 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $\begin{array}{r}52 \\ 31 \\ 14 \\ 3 \\ 3 \\ 3 \\ 2 \\ \hline\end{array}$ |
|  |  | 11 |  | 45 | 53 | 55 | 19 | 4 | 4 | 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 168 |
| 20 | 0 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0 |
| Total | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \\ & 4 \\ & 5 \\ & 6 \\ & 7 \end{aligned}$ |  |  |  | 1 <br> 1 | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ |  |  |  | $2$ | $\begin{aligned} & 3 \\ & 4 \\ & 2 \end{aligned}$ <br> 1 | $\mathbf{8}$ 2 1 1 2 1 1 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 21 7 7 2 3 1 2 |
|  |  |  |  | 2 | 2 | 2 | 2 | 6 | 6 | 2 | 10 | 16 | 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 43 |

Table 4.-(continued).


Table 4.-(continued).


Table 4.-(continued).


Table 4.-(continued)


EXPERIMENTS ON PACIFIC HALIBUT 23

Table 4.-(continued).


Table 4.-(continued).


Table 4.-(continued).


Table 4.-(continued).


Table 4．－（continued）．


Table 5. Calculated number of standard skates fished in statistical areas 9 to 36 for the years 1926-1963.*

| Year | Statistical Areas |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 1926 | 23373 | 63518 | 61541 | 37297 | 112783 | 21580 | 27611 |
| 1927 | 20008 | 62921 | 51887 | 33866 | 105470 | 22905 | 29795 |
| 1928 | 25381 | 65525 | 69320 | 41581 | 116038 | 26707 | 34707 |
| 1929 | 31814 | 74552 | 66435 | 40485 | 116448 | 40276 | 53069 |
| 1930 | 39021 | 76398 | 60225 | 43856 | 108292 | 39769 | 53295 |
| 1931 | 49105 | 88295 | 53470 | 38258 | 85282 | 34362 | 32280 |
| 1932 | 43251 | 76682 | 37268 | 26314 | 61988 | 22636 | 24679 |
| 1933 | 41143 | 55948 | 35765 | 26092 | 72773 | 21511 | 20242 |
| 1934 | 36170 | 49832 | 33504 | 37383 | 83398 | 19140 | 22745 |
| 1935 | 28111 | 48506 | 28982 | 27937 | 64715 | 17987 | 26752 |
| 1936 | 39083 | 52551 | 29975 | 30513 | 73463 | 24067 | 34494 |
| 1937 | 40662 | 43359 | 31742 | 36731 | 72218 | 24392 | 23226 |
| 1938 | 25236 | 53664 | 31915 | 25318 | 56373 | 17545 | 22778 |
| 1939 | 31973 | 87826 | 35597 | 37153 | 71140 | 14399 | 20795 |
| 1940 | 40010 | 71649 | 35152 | 40333 | 64402 | 18399 | 23463 |
| 1941 | 43247 | 65240 | 28104 | 25577 | 74845 | 20377 | 19497 |
| 1942 | 43848 | 62319 | 27000 | 22226 | 50603 | 15065 | 26107 |
| 1943 | 40930 | 57043 | 22476 | 22523 | 47982 | 12319 | 18711 |
| 1944 | 27318 | 44576 | 25108 | 20159 | 41514 | 15952 | 17914 |
| 1945 | 22109 | 45657 | 13256 | 27999 | 57828 | 13275 | 10589 |
| 1946 | 19941 | 41862 | 14740 | 35661 | 83974 | 14788 | 18977 |
| 1947 | 23832 | 39693 | 13492 | 29237 | 83555 | 12800 | 17943 |
| 1948 | 28031 | 40839 | 10304 | 27995 | 66522 | 12039 | 19394 |
| 1949 | 23964 | 35355 | 9021 | 32975 | 57790 | 11501 | 21988 |
| 1950 | 18636 | 29935 | 13867 | 46685 | 59424 | 8470 | 19094 |
| 1951 | 20102 | 42862 | 30125 | 39312 | 73768 | 14190 | 15331 |
| 1952 | 17585 | 28963 | 25039 | 34151 | 60368 | 18231 | 14464 |
| 1953 | 16517 | 22349 | 28967 | 31488 | 62048 | 12803 | 12992 |
| 1954 | 24178 | 44225 | 13163 | 24243 | 53593 | 8688 | 8931 |
| 1955 | 22607 | 45300 | 10638 | 14723 | 43218 | 6204 | 9600 |
| 1956 | 22044 | 40390 | 15333 | 21330 | 43810 | 11490 | 16836 |
| 1957 | 22398 | 30070 | 19994 | 27231 | 59005 | 14520 | 22200 |
| 1958 | 20133 | 26789 | 23256 | 18239 | 63705 | 17505 | 25548 |
| 1959 | 19130 | 24902 | 23686 | 19331 | 64743 | 14671 | 24451 |
| 1960 | 16900 | 31300 | 21716 | 13707 | 59594 | 9647 | 24114 |
| 1961 | 10842 | 29462 | 25066 | 18228 | 49998 | 13547 | 28016 |
| 1962 | 15637 | 21899 | 31124 | 18516 | 58945 | 17501 | 38173 |
| 1963 | 18207 | 23198 | 26347 | 18913 | 59551 | 18751 | 28816 |

[^1]Table 5.-(continued).

| Year | 16 | 17 | 18 | Statistical Areas 19 | 20 | 21 | 22 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1926 | 39693 | 16793 | 28225 | 12006 | 16904 | 10926 | 11029 |
| 1927 | 45254 | 18001 | 36337 | 18479 | 29282 | 16082 | 15317 |
| 1928 | 46144 | 17271 | 34428 | 19129 | 29216 | 21633 | 22693 |
| 1929 | 74221 | 29674 | 49066 | 16732 | 24380 | 16592 | 14753 |
| 1930 | 72769 | 25376 | 48722 | 19040 | 24789 | 15605 | 17291 |
| 1931 | 60920 | 17252 | 44555 | 18625 | 20291 | 13970 | 6647 |
| 1932 | 57172 | 25565 | 33317 | 14170 | 23903 | 11225 | 11777 |
| 1933 | 58162 | 23400 | 44610 | 19654 | 27485 | 10740 | 13398 |
| 1934 | 44353 | 16211 | 35489 | 20987 | 24020 | 12608 | 10261 |
| 1935 | 35496 | 10660 | 48541 | 26078 | 22064 | 7005 | 9840 |
| 1936 | 39352 | 20521 | 59129 | 20883 | 23355 | 11003 | 11591 |
| 1937 | 43732 | 18207 | 59591 | 11386 | 19269 | 9678 | 7828 |
| 1938 | 38556 | 15059 | 54002 | 13565 | 18143 | 9278 | 7511 |
| 1939 | 39057 | 17979 | 60003 | 9781 | 15749 | 8318 | 5500 |
| 1940 | 38887 | 24930 | 50716 | 16110 | 15669 | 8516 | 6014 |
| 1941 | 36064 | 18196 | 38862 | 23044 | 14419 | 5293 | 2112 |
| 1942 | 36474 | 19257 | 32442 | 15614 | 15203 | 5461 | 4506 |
| 1943 | 36961 | 18319 | 28481 | 6688 | 15847 | 5061 | 6496 |
| 1944 | 44873 | 25151 | 33714 | 4896 | 9770 | 5004 | 6270 |
| 1945 | 40267 | 27372 | 38215 | 4662 | 6392 | 2898 | 2060 |
| 1946 | 42767 | 26015 | 38049 | 10325 | 17252 | 5594 | 4014 |
| 1947 | 42190 | 21530 | 49800 | 25425 | 16298 | 5088 | 6243 |
| 1948 | 37972 | 20377 | 30348 | 14229 | 13948 | 6372 | 5606 |
| 1949 | 36079 | 19903 | 31241 | 9150 | 18007 | 8135 | 8859 |
| 1950 | 31308 | 14232 | 27900 | 8331 | 14976 | 9076 | 10631 |
| 1951 | 30295 | 13035 | 20447 | 6279 | 11715 | 10218 | 12539 |
| 1952 | 26352 | 15780 | 18962 | 11663 | 22824 | 11957 | 10775 |
| 1953 | 20937 | 15000 | 17007 | 11059 | 18072 | 7997 | 7862 |
| 1954 | 24406 | 16946 | 23421 | 11587 | 24717 | 6046 | 9229 |
| 1955 | 24465 | 13518 | 21175 | 13976 | 1858] | 5817 | 9364 |
| 1956 | 37347 | 20905 | 20545 | 9637 | 14318 | 6953 | 9668 |
| 1957 | 35846 | 20675 | 19447 | 10826 | 8295 | 5995 | 6287 |
| 1958 | 33117 | 17443 | 20019 | 10191 | 16444 | 6095 | 6727 |
| 1959 | 29800 | 21250 | 18204 | 8715 | 17323 | 6132 | 8788 |
| 1960 | 40533 | 24166 | 23110 | 6610 | 7006 | 6917 | 8118 |
| 1961 | 38870 | 24567 | 19959 | 6983 | 8714 | 5164 | 7860 |
| 1962 | 47982 | 27059 | 19814 | 9827 | 8531 | 5427 | 6475 |
| 1963 | 36781 | 24741 | 19315 | 6268 | 10682 | 6342 | 8389 |

Table 5.-(continued).

| Year | Statistical Areas |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 23 | 24 | 25 | 26 | 27 | 28 | 29 |
| 1926 | 9593 | 25319 | 32778 | 35812 | 25800 | 48924 | 23982 |
| 1927 | 10894 | 24505 | 38454 | 37379 | 26333 | 42426 | 36626 |
| 1928 | 14548 | 24591 | 42097 | 47433 | 31661 | 48415 | 28037 |
| 1929 | 12296 | 30264 | 47210 | 47907 | 36127 | 56021 | 46507 |
| 1930 | 6970 | 32006 | 41432 | 47403 | 32154 | 49479 | 37107 |
| 1931 | 6455 | 12092 | 29365 | 27346 | 32628 | 30441 | 31058 |
| 1932 | 4327 | 14606 | 36770 | 28191 | 24660 | 26700 | 21742 |
| 1933 | 7424 | 18164 | 44867 | 32144 | 25255 | 24447 | 23202 |
| 1934 | 3937 | 12660 | 39384 | 27308 | 32859 | 26688 | 31485 |
| 1935 | 4283 | 11861 | 33307 | 21281 | 22787 | 24910 | 27982 |
| 1936 | 5453 | 15537 | 30358 | 21761 | 22967 | 21882 | 29925 |
| 1937 | 2846 | 11728 | 33871 | 15451 | 25507 | 21722 | 23931 |
| 1938 | 3521 | 13689 | 28882 | 16665 | 21870 | 20041 | 21420 |
| 1939 | 2904 | 10750 | 36323 | 21551 | 24946 | 16361 | 18004 |
| 1940 | 4160 | 17520 | 34579 | 32450 | 24148 | 18021 | 17303 |
| 1941 | 3243 | 16584 | 30469 | 27068 | 32113 | 18473 | 28411 |
| 1942 | 1825 | 13982 | 31357 | 25518 | 20629 | 23832 | 25679 |
| 1943 | 4388 | 13193 | 23118 | 31814 | 18149 | 27400 | 26505 |
| 1944 | 1449 | 11068 | 21740 | 27410 | 27661 | 21447 | 17570 |
| 1945 | 2896 | 10359 | 31091 : | 40202 | 24079 | 23363 | 23846 |
| 1946 | 6085 | 12576 | 28309 | 47691 | 20958 | 20380 | 19145 |
| 1947 | 10296 | 15802 | 14897 | 35331 | 18091 | 19400 | 23738 |
| 1948 | 8224 | 15778 | 31589 | 38089 | 19050 | 24076 | 19800 |
| 1949 | 12894 | 15658 | 26404 | 39005 | 26705 | 31329 | 24722 |
| 1950 | 15635 | 16554 | 36244 | 42588 | 29052 | 30482 | 23501 |
| 1951 | 13869 | 13729 | 53330 | 26332 | 23308 | 20375 | 21560 |
| 1952 | 13286 | 19839 | 34907 | 34287 | 17973 | 20882 | 11546 |
| 1953 | 12410 | 15197 | 35086 | 25148 | 13956 | 15890 | 10283 |
| 1954 | 15618 | 18843 | 41490 | 42565 | 22473 | 20871 | 10471 |
| 1955 | 14331 | 17376 | 38724 | 35616 | 15132 | 19738 | 13856 |
| 1956 | 10775 | 19389 | 30373 | 34703 | 17550 | 18745 | 23853 |
| 1957 | 13027 | 14216 | 38744 | 29016 | 21154 | 25730 | 21001 |
| 1958 | 6469 | 12812 | 37009 | 29019 | 17704 | 25475 | 12469 |
| 1959 | 13031 | 16216 | 34145 | 21182 | 15097 | 15432 | 11131 |
| 1960 | 9256 | 17442 | 30608 | 20269 | 15546 | 19820 | 24643 |
| 1961 | 10620 | 12002 | 37182 | 27304 | 13403 | 22126 | 26494 |
| 1962 | 13588 | 20575 | 40958 | 32294 | 20585 | 27279 | 20842 |
| 1963 | 11411 | 17350 | 47052 | 34217 | 15737 | 23451 | 28013 |

Table 5.-(continued).

| Year | Statistical Areas |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 30 | 31 | 32 | 33 | 34 | 35 | 36 |
| 1926 | 15922 | 3499 | 13177 | 1548 | 876 | 0 | 0 |
| 1927 | 22742 | 5683 | 15695 | 4224 | 803 | 0 | 0 |
| 1928 | 18758 | 3982 | 12809 | 1689 | 689 | 288 | 168 |
| 1929 | 29956 | 8219 | 23575 | 3516 | 973 | 0 | 0 |
| 1930 | . 46818 | 8598 | 14286 | 1509 | 1670 | 6365 | 6460 |
| 1931 | 23444 | 3071 | 12471 | 1131 | 5869 | 10187 | 4974 |
| 1932 | 19216 | 2952 | 6302 | 678 | 3098 | 1473 | 0 |
| 1933 | 12324 | 2905 | 3849 | 263 | 310 | 858 | 0 |
| 1934 | 11032 | 2076 | 2124 | 0 | 0 | 0 | 0 |
| 1935 | 8136 | 742 | 1374 | 0 | 0 | 0 | 0 |
| 1936 | 14363 | 1296 | 1356 | 0 | 0 | 0 | 0 |
| 1937 | 8995 | 2834 | 2156 | 0 | 0 | 0 | 0 |
| 1938 | 8236 | 3882 | 2157 | 0 | 0 | 0 | 0 |
| 1939 | 9019 | 2703 | 1769 | 0 | 0 | 0 | 0 |
| 1940 | 7113 | 2225 | 3551 | 0 | 0 | 0 | 0 |
| 1941 | 8153 | 2615 | 2584 | 0 | 0 | 0 | 0 |
| 1942 | 6846 | 1743 | 195 | 0 | 0 | 0 | 0 |
| 1943 | 13846 | 4321 | 7652 | 0 | 0 | 0 | 0 |
| 1944 | 9521 | 4767 | 13289 | 0 | 370 | 0 | 0 |
| 1945 | 18287 | 4094 | 17140 | 2241 | 1816 | 0 | 0 |
| 1946 | 13974 | 8520 | 16000 | 2893 | 3490 | 985 | 0 |
| 1947 | 10490 | 4866 | 7224 | 1649 | 1833 | 655 | 0 |
| 1948 | 14202 | 4184 | 15827 | 1055 | 3845 | 1204 | 527 |
| 1949 | 19697 | 1077 | 16443 | 431 | 1917 | 575 | 260 |
| 1950 | 13412 | 2047 | 15150 | 1284 | 537 | 453 | 0 |
| 1951 | 7993 | 3275 | 7471 | 733 | 377 | 0 | 620 |
| 1952 | 5511 | 2041 | 3952 | 1047 | 3808 | 797 | 1773 |
| 1953 | 6165 | 1491 | 3656 | 127 | 3281 | 783 | 657 |
| 1954 | 9287 | 2562 | 2327 | 234 | 3035 | 448 | 117 |
| 1955 | 9242 | 8249 | 10136 | 919 | 255 | 232 | 0 |
| 1956 | 19334 | 9888 | 4430 | 0 | 0 | 0 | 0 |
| 1957 | 16437 | 9576 | 8162 | 1391 | 542 | 0 | 0 |
| 1958 | 8400 | 12255 | 16027 | 879 | 169 | 0 | 29 |
| 1959 | 8460 | 8282 | 27374 | 6059 | 6908 | 761 | 0 |
| 1960 | 18999 | 10557 | 24820 | 4699 | 6781 | 319 | 936 |
| 1961 | 24870 | 18101 | 13239 | 4776 | 1667 | 161 | 471 |
| 1962 | 33479 | 21786 | 14887 | 6662 | 4462 | 1867 | 4813 |
| 1963 | 30462 | 26564 | 17310 | 11037 | 2189 | 1552 | 3185 |

## MORTALITY ESTIMATES

Estimates of the catchability coefficient per skate per square mile, the average gear density in skates per square mile, the average fishing mortality, the average total mortality and its variance are given for each experiment in Table 6. The average gear density is the arithmetic mean of the gear densities for the first three years of usable recoveries for each experiment. The average fishing mortality is the product of the catchability coefficient and the average gear density.

Verification of the above estimates is at least as important as their calculation. Lacking knowledge of the true values, a useful alternative is to test the estimates for characteristics to be expected from the parameters themselves. For example, if the disappearance component of total mortality is of the same magnitude for all experiments, total mortalities should vary between experiments in direct proportion with the fishing mortality rates. Hence, the expected relationship between fishing and total mortality would be a straight line with slope of unity and an intercept on the ordinate at a point which is an estimate of the average disappearance rate.

The data appear to describe the expected linear relationship as shown in Figure 2. The intercept of the fitted (solid) line is at 0.31 ( 95 percent confidence interval is $0.12<0.31<0.50$ ). The observed slope is 1.12 which is not significantly different from unit slope (broken line) with a P of 0.11 for the two-tailed test ( 95 percent confidence interval is $0.97<1.12<1.27$ ).

Since some tagging mortality and non-reporting loss of tags is expected and these losses would result in a slope greater than unity, a one-tailed test for slopes exceeding unity is probably more appropriate than the two-tailed or symmetrical test. The onetailed test yields a P of 0.06 which indicates that the observed slope exceeds unity by an amount unlikely to have occurred by chance. Another possible explanation in addition to the aforementioned tagging mortality and non-reporting loss is a decrease in q with age of the fish which was observed in some Area 2 experiments and will be discussed below.


Figure 2. Expected and observed relationship between estimates of fishing and total mortality rate.

Table 6. Estimates of catchability, gear density, fishing mortality, total mortality and variance of total mortality for 60 tagging experiments.

| Experiment Number | Catchability Coefficient (per skate/'mi2) | Average Gear Density (skates/mi2) | Average Fishing Mortality | Total Mortality <br> Average Variance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.0154 | 21.43 | 0.331 | 0.747 | 0.0106 |
| 2 | 0.0212 | 17.76 | 0.376 | 0.839 | 0.0091 |
| 3 | 0.0240 | 25.95 | 0.624 | 1.228 | 0.0043 |
| 4 | 0.0647 | 9.99 | 0.647 | 1.125 | 0.0020 |
| 5 | 0.0349 | 15.82 | 0.552 | 0.883 | 0.0063 |
| 6 | 0.0149 | 25.44 | 0.378 | 0.959 | 0.0218 |
| 7 | 0.0357 | 11.56 | 0.413 | 1.003 | 0.0168 |
| 8* | 0.0144 | 6.46 | 0.093 | 0.382 | 0.0016 |
| 9* | 0.0175 | 6.23 | 0.109 | 0.403 | 0.0044 |
| 10* | 0.0165 | 6.56 | 0.108 | 0.430 | 0,0014 |
| 11* | 0.0150 | 2.72 | 0.041 | 0.186 | 0.0133 |
| 12 | 0.0294 | 10.08 | 0.296 | 0.643 | 0.0102 |
| 13* | 0.0091 | 6.29 | 0.057 | 0.470 | 0.0142 |
| 14* | 0.0076 | 5.02 | 0.038 | 0.044 | 0.1266 |
| 15* | 0.0096 | 3.94 | 0.038 | 0.395 | 0.0046 |
| 16 | 0.0172 | 12.33 | 0.212 | 0.414 | 0.0009 |
| 17 | 0.0155 | 11.79 | 0.183 | 0.394 | 0.0051 |
| 18 | 0.0238 | 12.26 | 0.292 | 0.655 | 0.0019 |
| 19 | 0.0117 | 11.45 | 0.134 | 0.561 | 0.0047 |
| 20 | 0.0065 | 10.99 | 0.072 | 0.506 | 0.0107 |
| 21 | 0.0200 | 9.49 | 0.190 | 0.572 | 0.0042 |
| 22 | 0.0094 | 21.40 | 0.202 | 0.699 | 0.0487 |
| 23 | 0.0042 | 17.15 | 0.072 | 0.344 | 0.0103 |
| 24 | 0.0311 | 8.93 | 0.277 | 0.883 | 0.0049 |
| 25* | 0.0056 | 4.85 | 0.027 | 0.293 | 0.0017 |
| 26 | 0.0081 | 20.67 | 0.167 | 0.548 | 0.0051 |
| 27* | 0.0079 | 3.18 | 0.025 | 0.358 | 0.0016 |
| 28 | 0.0265 | 7.44 | 0.197 | 0.542 | 0.0100 |
| 29 | 0.0127 | 8.71 | 0.111 | 0.511 | 0.0009 |
| 30* | 0.0122 | 3.55 | 0.044 | 0.482 | 0.0090 |
| 31* | 0.0191 | 6.51 | 0.124 | 0.386 | 0.0050 |
| 32 | 0.0156 | 19.61 | 0.306 | 0.609 | 0.0037 |
| 33 | 0.0119 | 6.36 | 0.076 | 0.263 | 0.0148 |
| 34 | 0.0459 | 12.32 | 0.566 | 0.746 | 0.0010 |
| 35 | 0.0097 | 7.18 | 0.070 | 0.403 | 0.0061 |
| 36 | 0.0228 | 18.11 | 0.412 | 0.956 | 0.0113 |
| 37* | 0.0094 | 5.77 | 0.054 | 0.358 | 0.0019 |
| 38* | 0.0092 | 3.28 | 0.030 | 0.174 | 0.1941 |
| 39 | 0.0134 | 5.62 | 0.075 | 0.336 | 0.0033 |
| 40 | 0.0120 | 17.69 | 0.213 | 0.545 | 0.0017 |
| 41 | 0.0105 | 13.62 | 0.143 | 0.473 | 0.0041 |
| 42 | 0.0280 | 16.41 | 0.459 | 0.873 | 0.0030 |
| 43 | 0.0187 | 8.17 | 0.153 | 0.519 | 0.0012 |
| 44 | 0.0448 | 4.69 | 0.210 | 0.609 | 0.0014 |
| 45 | 0.0316 | 11.12 | 0.352 | 0.690 | 0.0085 |
| 46 | 0.0257 | 8.33 | 0.214 | 0.571 | 0.0089 |
| 47 | 0.0142 | 3.66 | 0.052 | 0.546 | 0.0075 |
| 48 | 0.0213 | 15.74 | 0.335 | 0.737 | 0.0374 |
| 49* | 0.0114 | 6.45 | 0.074 | 0.376 | 0.0073 |
| 50* | 0.0063 | 4.08 | 0.026 | 0.309 | 0.0080 |
| 51* | 0.0175 | 5.66 | 0.099 | 0.348 | 0.0032 |
| 52* | 0.0071 | 6.74 | 0.048 | 0.322 | 0.0076 |
| 53* | 0.0131 | 5.04 | 0.066 | 0.231 | 0.0026 |
| 54 | 0.0300 | 8.74 | 0.262 | 0.572 | 0.0030 |
| 55 | 0.0218 | 15.69 | 0.342 | 0.813 | 0.0019 |
| 56 | 0.0094 | 7.57 | 0.071 | 0.351 | 0.0095 |
| 57 | 0.0183 | 19.94 | 0.365 | 0.691 | 0.0410 |
| 58 | 0.0221 | 6.86 | 0.152 | 0.498 | 0.0022 |
| 59 | 0.0180 | 8.53 | 0.153 | 0.548 | 0.0024 |
| 60* | 0.0101 | 4.98 | 0.050 | 0.292 | 0.0061 |

* Area 3 experiments

The relationship between total mortality and fishing mortality was examined for Area 2 and Area 3 experiments separately to test the comparability of the data from the two areas. The resulting slopes were 1.03 and 0.88 respectively, neither of which were significantly different from unit slope. Thus the apparent difference from unit slope is obtained only with the combined data. It is concluded that total and fishing mortalities are linearly related as assumed in the model and that there is no statistically convincing evidence of non-reporting loss of tags in the available data.

The intercepts for the regression lines for the two areas taken separately were 0.34 and 0.30 respectively and these were not statistically different from each other or from the 0.31 obtained from the combined data. Thus the average disappearance of tags which includes natural mortality and shedding loss of tags is essentially the same in the two areas. The larger estimate of disappearance for Area 2 experiments could be attributed to trawl recoveries but there is no statistical justification to support this possibility. On the other hand these values appear large for a long-lived species, and they are larger than expected from previous estimates of natural mortality of 0.20 (IPHC, 1960) and shedding loss of 0.02 (Myhre, 1966).

## REPRESENTATIVENESS OF ESTIMATES

Constant catchability is a key assumption in the foregoing analysis. This assumption is deemed satisfied within an experiment if some average catchability exists for all individuals for the duration of the experiment. It is not necessary that catchability be the same for all experiments, only that it be constant within experiments.

Evidence suggesting that catchability differs by size of fish was given by Thompson and Herrington (1930) and by Kask (1935) who showed that percentage recovery of tagged fish differs by size of the fish at the time of tagging. Further evidence of this difference was obtained from four large tagging experiments, two


Figure 3. Relationship between estimate of catchability and length at tagging for Area 2 experiments (solid lines; experiments 44 and 54) and Area 3 experiments (broken lines, experiments 30 and 31).
from each of Areas 2 and 3. Each experiment was divided into groups of 200 to 400 individuals by length at tagging and catchability was then estimated for each group. The resulting estimates are plotted against the mean length for the group in Figure 3. The point plotted at 92 centimeters for experiment 44 is probably aberrant.

The two Area 2 experiments ( 44 and 54) show a declining trend in catchability with increase in size while the catchabilities for the Area 3 experiments ( 30 and 31) are fairly uniform with respect to size. In fact, there appears to be little difference in catchability between the 4 experiments for fish over 100 centimeters long at tagging. However, the modal size of Area 2 fish is usually about 80 centimeters long which may explain the higher catchability for Area 2 experiments. Still to be explained is the reason for the higher catchability of small fish in Area 2.

The difference in catchability between small and large fish in Area 2 suggests the possibility of a decrease in catchability for these fish as they grow to larger size. Such a change would result in an overestimation of both catchability and total mortality but the latter would be most affected. This type of error would reach important levels only in experiments in which small fish were a substantial proportion of the tagged sample and then only if small fish were substantially more catchable than larger fish in the same experiment. This type of error may have occurred in some of the experiments described above but it does not appear to be a serious problem.

Differences in catchability also occur between tagging locations as shown in Figure 4 which relates catchability to statistical area of tagging for the 60 experiments. Catchability is highest in the waters off British Columbia and declines to the north and west. This trend is consistent with the shift from smaller fish in Area 2 to larger fish in Area 3 but size does not appear to explain all of the difference. Also noteworthy is the greater range of catchabilities shown for the southern areas. This may indicate that the halibut in these areas are less uniformly distributed than are those in the western areas.


Figure 4. Relationship between estimates of catchability of halibut and statistical area of tagging.

The possibility of an historical change in catchability was tested using only experiments from statistical areas 9 to 13 (Table 1). These experiments were grouped into three 10 -year periods starting with 1925 . The mean catchabilities for the respective periods were $0.023,0.017$ and 0.021 . The number of experiments in each group were 6,4 and 25 respectively. Judging from the similarity of the group means and the variability of the individual estimates within each group the data provide no evidence of a change in catchability with time within the region tested.

From the above comparisons it is apparent that much of the difference in catchability between experiments is attributable to differences in the size of fish tagged and the tagging location. Such differences present no particular problem in estimating the fishing and total mortality experienced by a group of tagged fish. However, the projection of these estimates to a larger untagged population requires that the composition of the tagged and untagged population be the same. Although this requirement is probably reasonably well satisfied for most experiments described herein, it cannot be assured since the tagged individuals were not a deliberately stratified sample of the total population.

## DISCUSSION

In past analyses, fishing mortality estimates from Area 3 tagging experiments were substantially lower than those from Area 2 experiments (IPHC, 1960). In the present analysis, Area 3 experiments not only exhibit lower fishing mortality estimates but there appears to be a declining trend in fishing mortalities from east to west as seen in Figure 5. This difference is difficult to reconcile with empirical evidence that the halibut stocks in both areas were producing yields at or close to their respective maximum sustained yield levels (IPHC, 1960; Chapman, Myhre and Southward, 1962). If the yield of halibut from Area 3 cannot be materially increased by increasing the fishing intensity then either the fishing mortality rates computed for the two areas


Figure 5. Relationship between estimates of fishing mortality and statistical area of tagging.
are not comparable or the productivity of halibut in Area 3 is less than in Area 2 or both.

Evidence suggesting a lack of comparability between Area 2 and Area 3 catchability estimates was noted above. First, the Area 2 catchabilities were greater than those for Area 3, particularly for the smaller fish which dominate the Area 2 catch. Secondly, the range of catchabilities for Area 2 experiments was substantially greater than those for Area 3. Such a wide range of catchabilities may indicate that the vulnerability of Area 2 halibut to fishing is markedly variable between fishing grounds. Since for most Area 2 experiments tagging and fishing tended to be concentrated on grounds where halibut are concentrated, the resulting estimates of catchability, may be too high for Area 2 halibut in general. Any such lack of comparability of catchability estimates for Areas 2 and 3 must be recognized in any comparison of the general level of utilization of the halibut of the two areas.

This is not to imply that the optimum level of fishing mortality must be equal in the two areas. Any difference in their level of productivity will result in differences in their optimum level of fishing mortality. The productivity of these areas depends upon the dynamic relationship between such population characteristics as growth, recruitment, migration, natural mortality and fishing mortality. Area 3 apparently had a growth rate lower than in Area 2 in the early years of the fishery (Thompson and Bell, 1934) but this does not appear to be the case in recent years (IPHC, 1960; Southward, 1967).

The migration of halibut from Area 3 to Area 2 exceeds that in the opposite direction as seen in Table 4 and as was reported by Thompson and Herrington (1930). As suggested by Dunlop, et al (1964), this net easterly migration would constitute a form of recruitment from western to eastern grounds. While such recruitment would contribute to the sustainable catch from the eastern grounds, it would result in a reduction in the sustainable catch from the western grounds. Further study of this problem is required to determine if the magnitude of the net contribution of halibut from western to eastern grounds is sufficient to influence the level of fishing mortality sustainable by the halibut of the two areas.

## VARIANCES AND CONFIDENCE INTERVALS OF TOTAL MORTALITY ESTIMATES

The variance of a statistic provides valuable information on the amount of confidence which can be justifiably placed in that statistic. It is, therefore, a useful weighting factor when data of varying dependability are being analyzed.

Within each experiment the number of recoveries was expected to decrease from year to year in approximately the same manner as the number of tagged fish in the population. Thus it was expected that the reliability of the dependent variable in equation (6) would decrease with passage of time. The variance of the data for each year was not available so some alternative measure of reliability was required.

According to Chapman (1956) the variance of $\operatorname{Ln}\left(\mathbf{n}_{\mathbf{i}} / \mathrm{N}_{0}\right)$ is approximately proportional to the reciprocal of $n_{i}$ for $n_{i}>10$. Thus, weighting the dependent variable by $n_{i}$ is justified for large $n_{i}$. There remains the question of whether weighting by $n_{i}$ gives too little weight to observations based on small $n_{i}$. To test the effect of more uniform weighting, total mortalities were recomputed while weighting observations by $V \mathrm{n}_{\mathrm{i}}$. The resulting variances of the total mortality estimates were 18 percent greater
on the average than with weighting by $n_{i}$. From this it was concluded that weighting by $n_{i}$ was justified.

The variances of the estimates of total mortality also provide a basis for deciding how the value of the tagging program can be maximized for the time and money invested. However, the standard deviation is more appropriate for consideration of confidence intervals than the variance.

The relationship between the number of fish tagged in each experiment and the standard deviation of the resulting estimates of total mortality is shown in Figure 6. An eye-fitted line was drawn through the data to reflect the general trend of the relationship. The broken segment on the left end of the line projects the anticipated relationship for small members of tagged fish.

The above relationship agrees in general with expectation based upon an equation for the large-sample variance of total mortality given by Chapman (1961). That equation is

$$
\begin{equation*}
V^{2} Z_{i}=\frac{1}{n_{i}}\left[Z_{i}-2-\triangle_{i}^{2} e^{-Z_{i} \Delta_{i}\left(1-e^{\left.-Z_{i} \triangle_{i}\right)^{-2}}\right]^{-1}}\right. \tag{8}
\end{equation*}
$$

where $\triangle_{i}$ is the duration of the recovery period. Since, for a given experiment, $n_{i}$ varies directly with the number tagged and $\triangle_{i}$ increases at a decreasing rate with increase in the number tagged, the variance is expected to decrease continuously with increase in releases. There is, therefore, no point at which additional tagging would fail to produce at least a proportionate decrease in the variance of the total mortality estimate.

The relationship between the standard deviation of the total mortality and numbers tagged will have a similar form except that the standard deviation does not decrease in inverse proportion to the numbers tagged. For example, an increase in numbers tagged from 200 to 1200 (a six-fold increase) results in approximately a 50 percent reduction in the observed standard deviation of the total mortality estimate.


Figure 6. Observed relationship between the effective number of fish tagged and the standard deviation of the estimate of total mortality.

From the shape of the relationship in Figure 6 it is concluded that experiments involving fewer than 200 tags released are highly unreliable on the average and that the expense of releasing additional tags is well justified. On the other hand, the additional precision gained by tagging more than 400 fish in a single experiment is not justified unless either the additional tags can be released at little or no expense or a small percentage recovery is anticipated. Generally speaking, more information would be obtained if the tagging vessel would move to a new location and start a new experiment after releasing about 300 tags at one place. The average of several such estimates would provide more information than a single estimate derived from the same total number of releases.

Most of the cost of tagging halibut is fixed and, hence, independent of the number of fish tagged. Thus the cost per tagged fish will vary roughly in inverse proportion to the availability of taggable fish. From this standpoint the least expensive procedure would be to tag where halibut are concentrated.

On the other hand, "spot" or "cluster" tagging may lead to atypical mortality estimates since the commercial halibut fleet also tends to frequent locations where halibut are concentrated. This would be a serious problem except that halibut tend to disperse so the tagged members become distributed through the population. Also, the operator of the tagging vessel is not so enlightened as to invariably select fishing locations where halibut are concentrated.

Theoretically, the ideal tagging procedure is to distribute tagging effort over a predetermined grid of equally spaced stations, thus assuring the distribution of tagged members through the total population and hence the representativeness of the tagged members. Conceivably the quality of the data from grid tagging could more than warrant the added cost of the operation over that of spot tagging. At least this was the reasoning under which the Commission embarked on a program of grid tagging in 1963. Whether the value of the additional information provided by grid tagging will justify the additional cost remains to be seen.

## SUMMARY

Sixty halibut tagging experiments conducted between 1925 and 1955 from Cape Scott, Vancouver Island, to Shumagin Islands, Alaska, were used to estimate fishing and total mortality for fully-recruited fish by the method of Gulland (1963). The slope of the regression line relating corresponding estimates of total and fishing mortality was found to be 1.12 which was not statistically different from the expected unit slope. The same relationship provided an estimate of 0.31 for all components of total mortality other than fishing. Similar results were obtained when the same analysis was conducted with Area 2 and Area 3 experiments separately.

Comparisons of catchabilities for halibut of different size at tagging indicated that halibut less than 100 centimeters long at tagging in Area 2 have a higher catchability than do the larger fish in that area and also higher than either large or small fish tagged in Area 3. Catchabilities for halibut tagged in British Columbia waters were higher than for those tagged to the north and west. Part of this difference may be due to the smaller average size of halibut in British Columbia waters.

Catchability estimates for that part of Area 2 lying between Vancouver Island and Dixon Entrance in British Columbia were tested for differences between 3 successive 10 -year periods beginning with 1925 . No evidence of a temporal change in catchability was found for this region.

Area 3 experiments yielded lower estimates of fishing mortality than did Area 2 experiments. Since other analyses have indicated that the halibut of both areas are being fished at or near their maximum sustained yield level, it is concluded that either the fishing mortality estimates lack comparability or the halibut of the two areas have different levels of productivity or both.

The variance and standard deviation of the total mortality estimates were related to the number of fish tagged. From the shape of this relationship it was concluded that a tagged sample of about 300 fish would usually produce estimates with acceptable variances. A larger sample size probably would not produce as much information as if the additional tagging effort was used in a new experiment at a different location.

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[^0]:    *The unit of fishing effort in the Pacific halibut fishery is called a skate. The standard skate as defined by the Commission consists of 300 fathoms (1800) feet of groundline with 120 hooks spaced at equal intervals.

[^1]:    *In calculating effort for 1926 to 1928, the total catch for groups of statistical areas was allocated to individual areas in accord with the average distribution in the 1929 to 1931 period.

